

This picture shows an Equilateral Triangle ABE in a Square $A B C D$.
$A$ point $F$ is on the line $B C$ such that $E C=E F$.
What is the angle BEF?

Answer to Math4Fun question

$\angle E B C=90^{\circ}-60^{\circ}=30^{\circ}$.
$E B=A B=B C$ so, triangle $E B C$ is isosceles.
Hence $\angle \mathrm{BCE}=1 / 2(180-30)^{\circ}=75^{\circ}$
$\mathrm{EC}=\mathrm{EF}$, so triangle EFC is isosceles and $\angle \mathrm{EFC}=75^{\circ}$
$\angle \mathrm{EFB}=(180-75)^{\circ}=105^{\circ}$ and $\angle \mathrm{FBE}=30^{\circ}$,
so $\angle B E F=(180-105-30)^{\circ}=45^{\circ}$

