Maths puzzle from Ken Smith

ABC is an Equilateral Triangle. DEF is an Isosceles Triangle within ABC as shown such that EF=one third of CB and parallel to it. What is the Ratio of the area of DEF to the area of ABC ?



Solution

Let height of triangle ABC be "h" and the length of base BC = "b" Therefore area of ABC = $\frac{1}{2}$ of bh EF=CB/3 = b/3 and height of triangle DEF = $\frac{2h}{3}$ Therefore area of triangle DEF = $\frac{1}{2} \times \frac{b}{3} \times \frac{2h}{3} = \frac{bh}{9}$ Therefore Ratio of areas = $\frac{bh}{9} / \frac{bh}{2} = \frac{2}{9}$