## Maths puzzle from Ken Smith

$A B C$ is an Equilateral Triangle.
DEF is an Isosceles Triangle within ABC as shown such that $E F=$ one third of $C B$ and parallel to it.

What is the Ratio of the area of DEF to the area of $A B C$ ?


## Solution

Let height of triangle $A B C$ be " $h$ " and the length of base $B C=$ " $b$ "
Therefore area of $A B C=1 / 2$ of $b h$
$\mathrm{EF}=\mathrm{CB} / 3=\mathrm{b} / 3$ and height of triangle DEF $=2 \mathrm{~h} / 3$
Therefore area of triangle DEF $=1 / 2 \times b / 3 . \times 2 h / 3=b h / 9$
Therefore Ratio of areas $=(b h / 9) /(b h / 2)=2 / 9$

